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# Size-dependent piezoelectric coefficient $d_{33}$ of PbTiO<sub>3</sub> nanoparticles

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#### Abstract

Size-dependent piezoelectric coefficient  $d_{33}(D)$  (*D* shows particle diameter) for small ferroelectrics is modeled in this paper. It is found that taking account of size effect is essential in understanding piezoelectric characteristics of nanoferroelectrics. The model prediction is in good agreement with the experimental results for PbTiO<sub>3</sub> nanoparticles, where  $d_{33}(D)$  increases correspondingly as *D* decreases. In addition, the size effect of the dielectric susceptibility coefficient  $\eta_{33}(D)$  is also predicted since  $\eta_{33}(D) \propto d_{33}(D)$  is considered. Our model estimations for  $\eta_{33}(D)$  function are consistent with other theoretical evidences.

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# 1. Introduction

The continuous advance in microelectronics and communications is leading to the miniaturization and integration of ferroelectric components. On the other hand, higher strain piezoelectric materials also have drawn much attention for the fabrication of microelectrictromechanical systems, such as microactuators, pressure transducers, and high-frequency ultrasound transducers [1-3]. As a candidate, PbTiO<sub>3</sub> nanoparticles are extensively used in the piezoelectric transducer [1-3], and can well satisfy the technological requirements mentioned above since the piezoelectric coefficient of PbTiO<sub>3</sub> is observed to increase with size dropping [2]. It is known that, nanoparticles with higher surfaceto-volume ratio, have substantial difference of physical, chemical and mechanical properties from their counterparts in bulk materials. Therefore, piezoelectric property is also a function of D (D denotes particle diameter) and it plays an important role in determining the application of nanoferroelectrics.

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PbTiO<sub>3</sub> with perovskite structure, is cubic and paraelectric above the Curie temperature, while tetragonal structure is stable below the Curie temperature. Since the polarization direction of the tetragonal PbTiO<sub>3</sub> with nonzero dipole moment ( $P_1 = P_2 = 0$ ,  $P_3 = P_s \neq 0$ , where the subscripts denote polarization axis directions and  $P_s$  is spontaneous polarization) is the desired one in devices for technological applications, and expected to be stable and the largest [4-6], the investigation on the piezoelectric coefficient  $(d_{33})$  in this direction becomes valuable and possible. To clarify the size effect on ferroelectric properties such as phase transition, many efforts have been made [5,7-10]. They show that Curie temperature shifts towards lower temperature with the decrease of D, and the corresponding spontaneous polarization P<sub>s</sub> also decreases. Furthermore, Akdogan et al. [2] have found that electrostrictive coefficients of PbTiO<sub>3</sub> particles exhibit an order of magnitude increase when the size decreases to nanoscale, which leads to an increase of the intrinsic piezoelectric coefficient  $d_{33}$ . They attributed this abnormal behavior into the inherent cooperative nature of ferroelectricity arising from long-range dipolar coupling. However, quantitative explanation for  $d_{33}$  variation with size is rarely reported. In this work, the model for  $d_{33}(D)$  function of PbTiO<sub>3</sub> particles is established.

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The model predictions are used to compare with the evidences obtained from experiments.

# 2. Model

According to the Landau–Ginsburg–Devonshire (LGD) theory for tetragonal PbTiO<sub>3</sub> ferroelectrics, piezoelectric coefficient  $d_{33}$  is expressed as [11],

$$d_{33} = 2\varepsilon_0 \eta_{33} Q_{11} P_{\rm s} \tag{1}$$

where  $\varepsilon_0$  is permittivity of free space,  $Q_{11}$  shows electrostrictive coefficient, and  $\eta_{33}$  denote relative dielectric susceptibility coefficient and can be written [11],

$$\eta_{33} = \left[ \left( 2\alpha_1 + 12\alpha_{11}P_s^2 + 30\alpha_{111}P_s^4 \right) \varepsilon_0 \right]^{-1} \tag{2}$$

where  $\alpha_1$ ,  $\alpha_{11}$ , and  $\alpha_{111}$  are the dielectric stiffness and higherorder stiffness coefficients which can be obtained from the available thermodynamic amounts.

To determine  $d_{33}$  values, the parameters concerned in Eq. (1) should be known. As shown in Refs. [12,13], there is a second-order relationship between  $P_s$  and  $Q_{11}$  via  $x_3 = Q_{11}P_s^2$  with  $x_3$  being elastic strains. Since both  $x_3$  and  $P_s$  are fundamentally related to atomic shifts ( $\Delta z$ ) with respect to the equilibrium positions in the cubic lattice,  $P_s$  (or  $x_3$ ) ~  $\Delta z$  is assumed [12,14]. As a result,  $Q_{11} \sim \Delta z^{-1}$  can be expected according to the above relationship. Taking the multiply of  $Q_{11}P_s$  in Eq. (1) as an ensemble for simplicity,  $Q_{11}P_s$  as a constant is considered. Therefore, in terms of Eq. (1), there exists an approximate relationship  $d_{33} \propto \eta_{33}$  where  $\varepsilon_0$  is assumed to be size-independent.

On the other hand, it is necessary to allow for the size effect of the parameters  $\alpha_1$ ,  $\alpha_{11}$ ,  $\alpha_{111}$  and  $P_s$  appearing in Eq. (2). In light of Curie–Wess law,  $\alpha_1$  is read,

$$\alpha_1 = (T - \theta) / (2\varepsilon_0 C) \tag{3}$$

where *T* is absolute temperature, *C* is Curie constant and  $\theta$  Curie–Weiss temperature. Since the tetragonal-cubic transition is first order in light of the thermodynamic considerations, the difference value of  $(T_C - \theta)$  being a constant is taken [13], where  $T_C$  is the Curie temperature. Therefore, by introducing size-dependent  $T_C(D)$  and  $\theta(D)$  functions, there will be:  $T_C(D)$ –



Fig. 1. A comparison for  $d_{33}(D)$  function of PbTiO<sub>3</sub> particles between model prediction in terms of Eq. (7) (solid line) and the experimental results (**1**) [2] at 298 K.

Table 1 The thermodynamic data of PbTiO<sub>3</sub>

Parameters	Quantity
$T_{\rm C}(\infty)$ (K)	765.4 [11]
$\theta(\infty)$ (K)	752 [11]
$T_{\rm C} - \theta$ (K)	13.4 [11]
$\alpha_1(\infty) \ (10^6 \text{ m F}^{-1}) \text{ at } T_{\rm C}$	5.045 [11]
$\alpha_{11} (10^7 \text{ m}^5 \text{ C}^{-2} \text{ F})$	-7.252 [11]
$\alpha_{111} (10^8 \text{ m}^9 \text{ C}^{-4} \text{ F})$	2.606 [11]
$P_{\rm s}(\infty) \ ({\rm C} \ {\rm m}^{-2}) \ {\rm at} \ 298 \ {\rm K}$	0.75 [11]
$d_{33}(\infty)$ (PC N <sup>-1</sup> ) at 298 K	79.1 [11]
$\eta_{33}(\infty)$ at 298 K	66.6 [11]
$S_0 (\text{J mol}^{-1} \text{ K}^{-1})$	2.3 [17]
$D_0 (\text{nm})$	13.8 [9]
$\varepsilon_0 C (10^{-6} \text{ K m}^{-1} \text{ F})$	1.3 <sup>a</sup>

<sup>a</sup>  $\varepsilon_0 C$  is determined by the Curie–Wess law in terms of Eq. (3) where *T* is taken as Curie transition temperature  $T_C$  and the value of  $\alpha_1$  is the value at  $T_C$ .

 $\theta(D) \approx T_{\rm C}(\infty) - \theta(\infty)$  with  $\infty$  denoting the bulk value.  $T_{\rm C}(D)$  has been proposed as [7],

$$\frac{T_C(D)}{T_C(\infty)} = \exp\left(-\frac{2S_0}{3R}\frac{1}{D/D_0 - 1}\right) \tag{4}$$

where  $S_0$  is the transition entropy from ferroelectric tetragonal phase to paraelectric cubic one, and *R* the ideal gas constant.  $D_0$ is defined as a critical particle size where the ferroelectric phase cannot exist or the Curie transition is absent. Combining Eq. (4) and the available expression for  $\theta(D)$  function,  $\alpha_1(D)$  is obtained,

$$\alpha_1(D) = [T + T_C(\infty) - \theta(\infty) - T_C(D)]/(2\varepsilon_0 C)$$
(5)

Although the study on size effects of  $\alpha_{11}$  and  $\alpha_{111}$  parameters are few, their temperature dependences have been investigated [11], showing that the temperature contribution to both  $\alpha_{11}$  and  $\alpha_{111}$  is small enough to be neglected. Moreover, as particle size decreases, the corresponding Curie temperature or melting temperature will decreases correspondingly. As a result, size decreasing can be regarded as working temperature enhancing to some extent. Based on the discussion above,  $\alpha_{11}$  and  $\alpha_{111}$  are supposed to be size-independent in this paper.



Fig. 2. Model prediction of  $\eta_{33}(D)$  for PbTiO<sub>3</sub> particles.

In addition, the contribution of surface layer to  $P_s$  becomes significant because the dipoles located at surfaces differ from that inside the materials and thus results in the alteration of  $P_s$ [15]. Size-dependent spontaneous polarization  $P_s(D)$  has been extended [10],

$$\frac{P_s(D)}{P_s(\infty)} = \exp\left(-\frac{S_0}{3R}\frac{1}{D/D_0 - 1}\right) \tag{6}$$

where the related parameters are same with that in Eq. (4). Based on the consideration above, an analytical expression for size-dependent intrinsic piezoelectric coefficient  $d_{33}(D)$  and the corresponding  $\eta_{33}(D)$  function can be determined,

$$\frac{d_{33}(D)}{d_{33}(\infty)} = \frac{\eta_{33}(D)}{\eta_{33}(\infty)} 
= \frac{2\alpha_1(\infty) + 12\alpha_{11}P_s^2(\infty) + 30\alpha_{111}P_s^4(\infty)}{2\alpha_1(D) + 12\alpha_{11}P_s^2(D) + 30\alpha_{111}P_s^4(D)}$$
(7)

where  $\alpha_1(D)$  and  $P_s(D)$  are determined by Eqs. (5) and (6) respectively.

#### 3. Results and discussion

Fig. 1 presents a comparison between the model prediction of piezoelectric coefficient  $d_{33}(D)$  at 298K in terms of Eq. (7) and the experimental results for PbTiO<sub>3</sub> particles, where the related parameters are listed in Table 1. The both are consistent each other. As shown in Fig. 1,  $d_{33}(D)$  increases with D decreasing, especially when D < 100 nm, and  $d_{33}(D) \rightarrow d(\infty)$  as  $D \rightarrow \infty$ .  $\eta_{33}(D)$  function is also shown in Fig. 2. Due to a lack of necessary experimental data obtained, a comparison between model prediction and experimental results fails. However, the trend of  $\eta_{33}$  with size is consistent with that of other theoretical estimations [2,16].

According to Eq. (7),  $d_{33}(D)$  and  $\eta_{33}(D)$  functions are related not only with size, but also with temperature. For bulk PbTiO<sub>3</sub>, Haun et al. [11] demonstrated that  $d_{33}(\infty)$  and  $\eta_{33}(\infty)$  increase with *T* rising due to the enhanced  $\alpha_1$ , which indirectly implies that  $d_{33}(D)$  and  $\eta_{33}(D)$ increase as *D* decreases, when the concerned *T* is fixed. By observing Eq. (7), the parameters related to determine  $d_{33}(D)$  are determined by thermodynamic quantities of a material, which are available from experiments. Thus, our model seems to be applicable for other ferroelectrics particle, such as  $BaTiO_3$ , if the relative parameters are known. Moreover, the success of Eq. (7) implies that the assumptions used in this paper are reasonable.

#### 4. Conclusion

In summary, size effect on the piezoelectric coefficient  $d_{33}$ (D) and dielectric susceptibility coefficient  $\eta_{33}(D)$  for PbTiO<sub>3</sub> particles is investigated, and can be determined as long as the relative thermodynamic parameters are clear. As the particle size decreases,  $d_{33}(D)$  and  $\eta_{33}(D)$  increase correspondingly. The obtained results are in agreement with the theoretical and experimental observations.

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